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Automated detection of circinate exudates in retina digital images using empirical mode decomposition and the entropy and uniformity of the intrinsic mode functions

Abstract: This work presents a new automated system to detect circinate exudates in retina digital images. It operates as follows: the true color image is converted to gray levels, and contrast-limited adaptive histogram equalization (CLAHE) is applied to it before undergoing empirical mode decomposition (EMD) as intrinsic mode functions (IMFs). The entropies and uniformities of the first two IMFs are then computed to form a feature vector that is fed to a support vector machine (SVM) for classification. The experimental results using a set of 45 images (23 normal images and 22 images with circinate exudates taken from the STARE database) and tenfold cross-validation indicate that the proposed approach outperforms previous works found in the literature, with perfect classification. In addition, the image processing time was <4 min, making the presented circinate exudate detection system fit for use in a clinical environment.

Keywords: automated detection; circinate exudates; classification; empirical mode decomposition; feature extraction; retina.

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Introduction

Diabetic retinopathy (DR) is the leading cause of preventable blindness in Western countries [7], and circinate exudates are an important sign in early DR. When they occur in the foveal area, the resulting damage results in blindness, and elsewhere, they can create severe vision problems. Hence, the detection of exudates is of primary

importance in early DR diagnosis and treatment. These lipid deposits due to vascular leakage appear in bright yellow in retina digital images, and many automated detection efforts have been devoted to them in the literature, using approaches based on spatial distribution features [1, 2, 9, 21, 22, 28, 36], morphology analysis [4, 14, 31, 34, 35], or segmentation [5–7, 10, 29, 30] as described below.

Osareh et al. [22] presented an automated system based on color normalization and local contrast enhancement, followed by fuzzy C-means clustering for image segmentation, and neural network (NN) classification. The neural network achieved 93.4% accuracy, 93% sensitivity, and 94.1% specificity on a dataset of 142 color images. Zhang and Chutatape [36] used local contrast enhancement, fuzzy C-means, and SVM to detect and classify bright lesions. The obtained sensitivity and specificity were 88% and 84%, respectively, on a dataset of 30 exudate images. Massey and Hunter [21] employed an algorithm based on the spatial clustering of objects and individual appearance to estimate the probability of individual objects being circinate exudate. The purpose of the study was to classify exudates as bright or dark retinal lesions. Their algorithm, called SAGE, achieved an AUC of 0.83 on a training set of 105 exudate images and a testing set of 12. It also led to a lower cross-entropy error (CEE) than NN and SVM for bright and dark lesions alike. Sanchez et al. [28] proposed a general approach based on context-based features, which takes into account the presence of anatomical landmarks and spatial relationship between candidates (exudates) of the same class. Feature selection was carried out by sequential forward floating selection (SFFS) to establish the 30 most discriminative features. Using a dataset of 69 normal and 75 abnormal images, the linear discriminant classifier achieved a free receiver operating characteristic (FROC) curve of 0.945. Agurto et al. [1] presented an algorithm to automatically classify images with pathologic features commonly found in diabetic retinopathy (DR) and age-related macular degeneration (AMD). Their algorithm used the amplitude-modulation

frequency-modulation (AM-FM) to define the features for characterizing normal and pathologic structures based on their pixel intensity, size, and geometry at different spatial and spectral scales. Then, a sequential backward elimination process was employed to measure the contribution of each feature in the improvement of classification accuracy. Those that did not improve the classification performance were eliminated from the initial feature set. The sequential backward elimination process was applied independently to each of the pathologic features of interest to obtain the image representation at each frequency band. Finally, the partial least-squares regression was used to find the relevant features that classify images as normal or abnormal according to ground truth. Using 2247 retinal digital photographs obtained of the eyes of 822 patients, the system achieved an average AUC of 0.89 for detection of DR and of 0.92 for detection of sight-threatening DR (STDR). In a similar work, Agurto et al. [2] employed the AM-FM technique to detect DR in retinal images. They used 120 regions of 40×40 pixels containing four types of lesions commonly associated with DR including microaneurysms, exudates, neovascularization on the retina, hemorrhages, normal retinal background, and normal vessels patterns. The texture feature vector contained the cumulative distribution functions of the instantaneous amplitude, the instantaneous frequency magnitude, and the relative instantaneous frequency angle from multiple scales. They concluded that there is a statistical differentiation of normal retinal structures and pathological lesions based on AM-FM features and that their methodology can be used in automatic DR screening. Grisan and Ruggeri [9] presented a system to detect and identify hemorrhagic (dark) lesions in retinal images in two steps. First, a local thresholding is applied to identify dark pixels in the image. Second, a density function is computed to identify cluster of pixels that are considered pixels belonging to candidate lesions. Their approach was tested on six images presenting dark lesions extracted from a database of 60 annotated images. The obtained detection rate was 94% the lesions present in an image. According to the authors, the hit-or-miss situation can compromise the clinical evaluation when an image presents only one lesion.

Flemming et al. [4] used multiscale morphological algorithms to obtain candidate exudates that were detected with 95.0% sensitivity and specificity using training and testing sets with, respectively, 139 normal images and 300 with exudates. Walter et al. [34] used high gray-level variation and morphological reconstruction techniques to find exudates and their contours. Moreover, the optic disc was detected with morphology filtering

techniques and the watershed transformation. Based on a small image dataset (15 normal and 15 with exudates), the proposed algorithm achieved a mean prediction accuracy of 92.4%, with 92.8% mean sensitivity. Sopharak et al. [31] used a set of morphological operators including threshold image using Otsu algorithm and morphological reconstruction by dilation for exudate detection. Based on a data set of 40 retinal images with 20 exudates and 20 normal, the obtained sensitivity and specificity were, respectively, 80% and 99.5%. Jaafar et al. [14] proposed an automated method based on an adaptive threshold and image partitioning. The image was split into a number of homogeneous sub-images, and a coarse segmentation based on the calculation of a local variation for all image pixels was used to outline the boundaries of all exudates. Finally, a morphological operation based on application of a logical intersection operator on the coarse segmentation and adaptive threshold results was used for final exudate detection. Using 76 normal and 114 abnormal images, the proposed approach achieved 99.5% accuracy with 91.2% sensitivity and 99.3% specificity. In another study, Welfer et al. [35] presented a methodology based on mathematical morphology to detect exudates in color eye fundus images. Their approach was based on two stages: 1) detection of candidate regions; 2) final exudate detection. The watershed transform was used to identify the optic disk boundary. Then, thresholding was applied to detect the candidate exudates. Finally, they used the foreground pixels of the candidate region to define a binary image where only the exudates are in the foreground. The system achieved an average sensitivity of 70.48% and an average specificity of 98.84% using a dataset of 89 images. According to the authors, the main drawback of their approach is that it has low specificity with and misclassification rate for images that do not contain exudates. In addition, there are many parameters to be tuned.

Giancardo et al. [7] used features based on color, wavelet decomposition, and automatic lesion segmentation to detect the presence of exudates in 169 randomly selected images from three different databases. Conditional entropy was applied to the initial features set to select the most informative ones, and subsequent classification was performed by support vector machines (SVM). Using receiver operating curve (ROC) analysis for performance evaluation, the achieved area under curve (AUC) was between 0.88 and 0.93 depending on the database used in the study. Garcia et al. [5, 6] combined global and adaptive histogram thresholding methods to segment regions with hard exudates. Then, a set of 18 visual and statistical exudate features was selected; it included color, shape features, region size, and compactness. The

subsequent validation with a radial basis function NN classifier achieved 92.54% accuracy, with 100% sensitivity and 81.48% specificity on a dataset of 27 normal and 90 abnormal images. Harangi et al. [10] used grayscale morphology to identify possible regions containing exudates. Then, an active contour-based method used to minimize the Chan-Vese energy was applied to extract the borders of the exudates. Fifty shape features were extracted for exudate discrimination, from which the most efficient 18 ones were selected based on the *t*-statistic. Using 89 color fundus images, a naïve Bayes classifier achieved 75% sensitivity. Soares et al. [30] used a method for exudate segmentation that was based on localization using scale-space extrinsic curvature and selection of the true ones using the local maxima blob response with dynamic threshold. Using a database of 46 abnormal and 43 normal images, the proposed system achieved a sensitivity of 97.07% and specificity of 99.90%. Sinthanayothin et al. [29] proposed an automated system for screening of diabetic retinopathy. The purpose was to detect retinal lesions defined as hard exudates, hemorrhages and microaneurysms. The recursive region growing segmentation (RRGS) algorithm was used for exudate detection. This algorithm identifies similar pixels within a region to determine the location of a boundary. Then, the Moat operator was applied to sharpen the edges of the red lesions against the red-orange background in the segmented image. The algorithm for exudate recognition was applied to 30 retinal images of which 21 contained exudates and nine were normal. In comparison with regions identified by the ophthalmologist, the obtained sensitivity and specificity were 88.5% and 99.7%, respectively.

Recently, the empirical mode decomposition (EMD) [13], an adaptive decomposition technique introduced for signal processing, was successfully applied for retina digital image processing and feature extraction for diagnosis purpose [18–20]. The EMD is a multiresolution technique introduced by Huang et al. [13] to perform the joint space-spatial frequency decomposition of a signal empirically by successive removal of elemental signals, the intrinsic mode functions or IMF, which represent the oscillatory modes of the original signal going from high- to low-frequency ranges. The obtained IMFs can then serve to represent the signal. The main advantage of using the EMD technique is that the input signal is analyzed without need to convolve it with a basis function as done for Fourier and wavelet transforms. In addition, the method is data-driven and, thus, self-adaptive. These features make EMD suitable for nonlinear and nonstationary data analysis.

As already mentioned, EMD had triggered a certain interest to use it for the automatic diagnosis of retina

digital images. For instance, the authors in [18] employed the discrete wavelet transform (DWT) and EMD to analyze retina images in the frequency domain through statistical features (namely, the mean, standard deviation, smoothness, third moment, uniformity, and entropy) that were extracted from the high-frequency components in the analyzed images. The purpose was to distinguish normal from any of various abnormal images. Three different ocular pathologies were considered: circinates, drusens, and microaneurysms (MA). Support vector machines (SVM) with polynomial and radial basis function kernel were used to classify the obtained feature vectors. The experimental results using the leave-one-out method (LOOM) for cross-validation showed the efficiency of the EMD-based features over the DWT-based ones. In addition, they indicated that a polynomial kernel performed better than the radial basis function kernel in the SVM classifier. In their subsequent work [19], the authors extended their previous work to classify normal versus artery, blots, circinates, drusens, and MA separately. The EMD-based statistical features helped detect circinate images with $95.11\% \pm 0.04$ accuracy. More recently, the authors in [20] ranked separately the extracted features from IMFs according to the *t*-statistic, the entropy statistic, the Battacharrayia statistic, ROC analysis, and principal component analysis (PCA). The selected features were then fed to support vector machines (SVM) to perform the normal-against-all classification task. Their results were that feature selection based on the Battacharrayia statistic gives the highest classification accuracy when using SVM with polynomial kernel: $96.54\% \pm 0.03$.

In general, all the surveyed works exhibited excellent classification performance, regardless of the approach and features used. However, they fail to achieve perfect recognition accuracy, and they follow rather complex procedures. For instance, morphology-based approaches require detecting the optic disc, watershed transformation, and subsequent morphological reconstruction. As a result, there are many parameters to tune and a large number of features to extract. This type of approach also carries a significant algorithmic complexity. Spatial transformation-based approaches require the estimation of probabilities of occurrence, which is difficult to achieve, and start with a large set of features that must be reduced by an appropriate dimensionality reduction technique. Finally, segmentation techniques are usually computationally intensive and require a smoothing and denoising image-preprocessing step in order to optimize the boundaries separating the regions.

In this work, we present a novel EMD-based approach that is simpler than the ones described in [18–20] and

that addresses the specific case of normal versus circinate image detection as done in [4–7, 14, 22, 31, 36]. Our approach consists of a four-step process that starts by converting the digital retina image to grayscale format and applying the contrast-limited adaptive histogram equalization (CLAHE) technique [24] to the result in order enhance contrast while mitigating noise over amplification during the process [3]. Converting the image to grayscale format avoids extracting features from each of the red, green, and blue channels, thus reducing the computation burden. The contrast-limited adaptive histogram equalization technique takes into account local image information to modify pixel brightness, with the result of an improved contrast between image components (Figure 2 provides an example). Overall, the first step is relatively simple and low in time consumption.

In the second step, the EMD is applied to the equalized-scale image for decomposition. Only the first two IMFs are determined as they contain most of the high-frequency components of the decomposed image, and these may efficiently characterize circinate exudates, which have well-defined edges. Higher-order IMFs with lower frequency content, such as the third IMF, are not helpful in this regard [31].

In the third step, the uniformity and entropy of each IMF are computed to form a feature vector; these variables were chosen for their reported effectiveness to characterize biological tissue [15, 16]. In our case, as circinates cause the proliferation of fibrous tissue and vitreous hemorrhagen [11], the structure of the cell components in the biological tissue is deteriorated, with the homogeneity of the biological texture affected. Because of this, the normal retina texture changes substantially and has a much less uniform pixel distribution. The uniformity and entropy statistics are appropriate to capture such variation.

In the final step, the feature vector is fed to support vector machines (SVM) [33] with quadratic kernel to perform classification. With respect to other classifiers, the SVM has the ability to avoid local minima in addition to being accurate [33]. The quadratic kernel is a global kernel that allows distant data points from each other to have also influence on the kernel values [32]. Moreover, it has proven its effectiveness in retina digital image classification [16, 18–20, 24].

The paper is organized as follows. The methodology is presented in the next section. This is followed by simulation results and then we conclude in the final section.

Materials and methods

The proposed automated system for circinate exudate detection in retina digital images is presented in Figure 1.

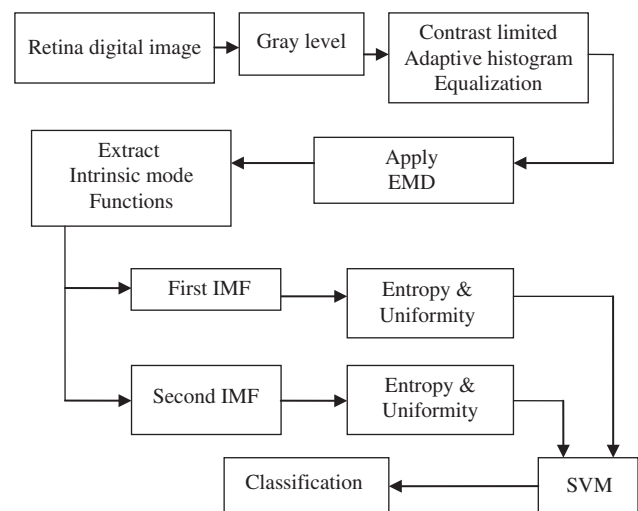


Figure 1 Block diagram of the proposed circinate exudates detection system.

As mentioned above, the design of the classification system consists of four steps:

1. The original retina digital image is converted to grayscale format before filtering with contrast-limited adaptive histogram equalization technique.
2. The first and second IMFs are extracted by EMD.
3. The entropy and uniformity statistics are computed from each extracted IMF to form a feature vector of four elements.
4. The feature vector serves as input for the SVM to classify normal image versus circinate exudates image.

Contrast-limited adaptive histogram equalization

Basic histogram equalization is a technique that spreads out the distribution of pixel intensities within an image, with enhanced contrast as a result. The stretching is typically accomplished by replacing each normalized pixel intensity value by its cumulative distribution in the original histogram, with the result of progressively increasing the difference between adjacent pixel intensities and of a wider distribution range between the brightest and darkest values. For an image I of size $n \times n$ and a histogram $h()$ defined by:

$$h(i) = \frac{n_i}{n^2}, \quad i \in [0, 1] \quad (1)$$

where i is a normalized pixel intensity, n_i the number of pixel with intensity i , and n^2 the total number of pixels in

the image, the histogram equalization algorithm creates a new image where each initial intensity i becomes i' such that:

$$i' = \sum_{k=0}^i h(k) \quad (2)$$

The above algorithm is efficient when the pixel distribution is homogeneous throughout the image; else, adaptive histogram equalization (AHE) offers a more efficient mapping that considers contextual pixel regions instead of the whole image, thus allowing sets of pixels with low contrast, but different ranges of intensity distributions, to become simultaneously enhanced for visibility [25, 37]. However, this comes at a high computational cost as a region histogram must be computed for each pixel in the image. One approach to lower the computational burden is to partition the image into a grid of contextual regions and use the mappings for the pixels located at the cell centers to interpolate those for the remaining pixels [23]. This amounts to ranking each pixel by its brightness in comparison to the other pixels in its contextual region and assigning a new brightness to it in proportion to its rank [23, 26]. Unfortunately, AHE worsens also the effect of noise when small contextual regions are used. Contrast-limited AHE minimizes the problem by limiting the dynamic range of the contrast enhancement process by clipping the height of the local histogram and using a maximum contrast enhancement factor [23] in the AHE algorithm.

The size of the partition grid (and subsequently the number of pixels in a contextual region) has an impact on the contrast enhancement outcome: small sizes (e.g., 8×8) lead to enhanced contrast as opposed to large ones. We used the same grid size as that of Ramlugun et al. [26], 8×8 , and the clip limit parameter was set to 0.01 in the CLAHE algorithm. Figure 2 provides an example of digital retina image with circinate exudates and the result of applying CLAHE to its grayscale representation.

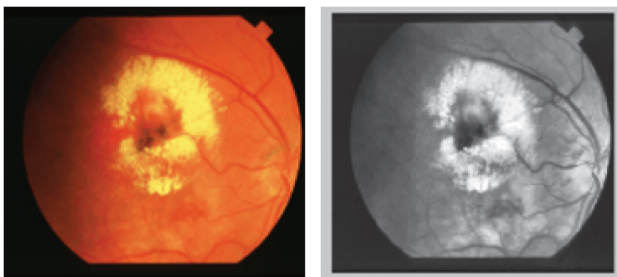


Figure 2 True color digital retina image with circinate exudates before (left) and after applying CLAHE to its grayscale version (right).

Empirical mode decomposition

The EMD [13] decomposes a signal into a sum of intrinsic mode functions or IMFs, each one satisfying two properties: (1) It has the same numbers of zero crossings and extrema, and (2) it is symmetric with respect to its local mean. The IMFs span a scale going from fine to coarse and are determined by an iterative procedure, the sifting algorithm. For a one-dimensional signal $s(t)$, the sifting process is performed as follows [13]:

1. Determination of all the local maxima M_p , $i=1, 2, \dots$, and minima m_k , $k=1, 2, \dots$, in $s(t)$;
2. Computation by interpolation – for instance, a cubic spline – of the upper and lower envelopes of the signal: $M(t)=f_M(M_p, t)$ and $m(t)=f_m(m_k, t)$;
3. Computation of the detail signal $d(t)=s(t)-\mu(t)$, where $\mu(t)=(M(t)+m(t))/2$ is the average of the upper and lower envelopes;
4. If $d(t)$ meets the properties of an IMF regarding symmetry and the number of extrema:
 - a. set the i th IMF as $IMF_i(t)=d(t)$
 - b. replace $s(t)$ with the residual $r(t)=s(t)-IMF_i(t)$; else, set $s(t)=d(t)$;
5. Iterate through steps 1–5 until residual $r(t)$ satisfies a given stopping criterion.

In practice, the stopping criterion for the sifting process consists of bounding the standard deviation (SD) calculated from two successive sifting results [13]:

$$SD(k) = \frac{\sum_{t=0}^T |d_{k-1}(t) - d_k(t)|^2}{\sum_{t=0}^T d_{k-1}^2(t)} < \varepsilon \quad (3)$$

where t is the time index, T is the length of $s(t)$, k the index of the k th detail signal, and ε is a given threshold. Alternatively, the sifting process stops when the residue function becomes monotonic or has one extrema so that no more IMF can be extracted. In the end, $s(t)$ is expressed as follows:

$$s(t) = \sum_{j=1}^N IMF_j(t) + r_N(t) \quad (4)$$

where N is the number of IMFs, which are nearly orthogonal to each other and have nearly zero means, and $r_N(t)$ is the final residue, which indicates the low frequency trend of $s(t)$.

The two-dimensional EMD follows the same process as the one-dimensional, and the two-dimensional IMFs

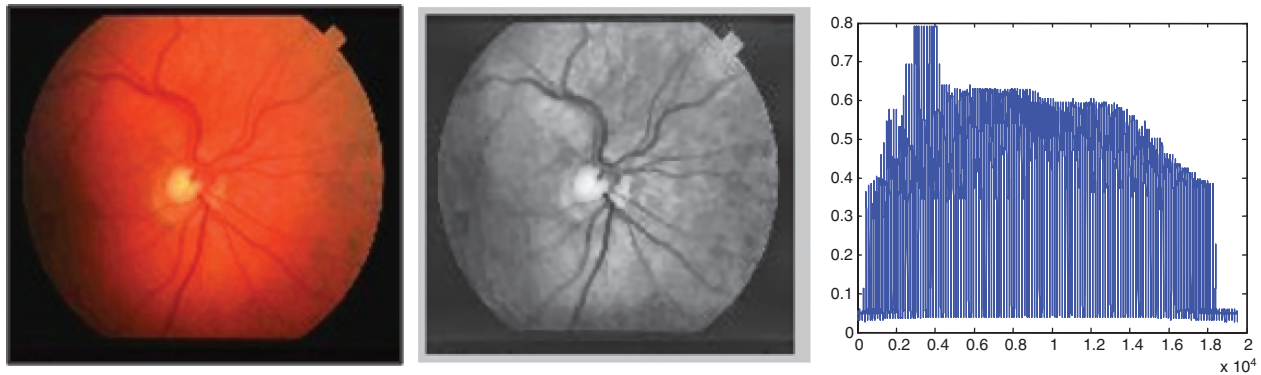


Figure 3 Normal retina color image (left), after applying CLAHE (middle), and CLAHE 1D signal representation (right).

are defined in a similar manner. In our study, we used a one-dimensional decomposition for computational efficiency. For an image of $n \times n$ pixels, the corresponding one-dimensional signal image is a vector with n^2 components resulting from concatenating the rows of the image starting from the top left corner. Then, the EMD algorithm is applied to this vector, and the processed image is reconstructed from it. To perform the EMD, we used the algorithm proposed by Rato et al. [27], which minimizes computation errors with four modifications of the original EMD algorithm. Figure 3 shows an example of normal retina color image, the result of applying CLAHE to its grayscale version, and the final one-dimensional signal

(1D) of the latter. Finally, Figure 4 shows the first 14 IMFs extracted from the same 1D signal.

Feature extraction and classification

Feature extraction

Two statistical textural features, entropy and uniformity, are extracted from the first and second intrinsic mode

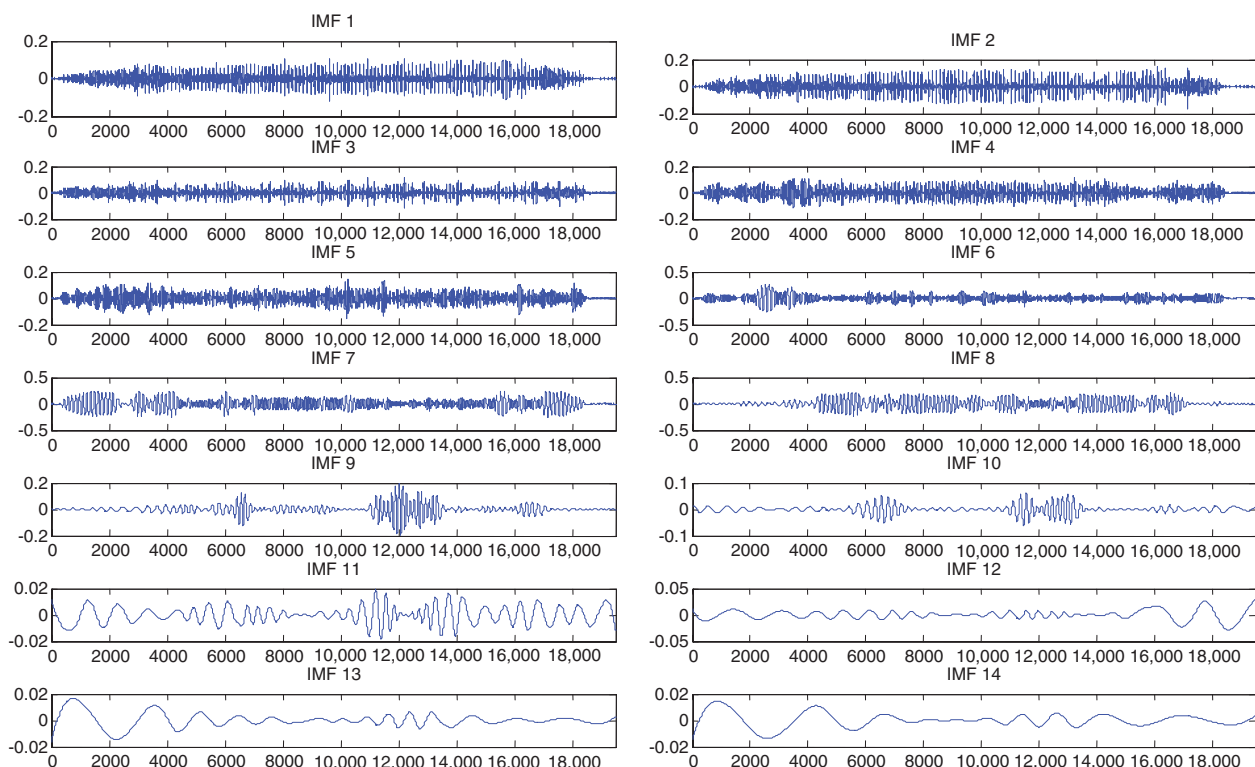


Figure 4 EMD decomposition of normal 1D signal shown in Figure 3 – right.

functions. Higher intrinsic mode functions, which contain lower frequency content, were ignored since we made the hypothesis that only the high-frequency elemental signals capture sudden and distinctive changes in the biological tissue. Initially, we started with a set of features that included the mean, standard deviation, kurtosis, third moment, uniformity, and entropy, but we obtained poorer classification results than when using the last two variables alone. This might be due to an antagonistic interaction between predictive variables where general statistics such as the removed features are detrimental to the predictive power of more focused “structural” statistics such as entropy and uniformity.

Entropy and uniformity have already been shown to be effective at distinguishing different types of biological tissues [17]. The former measures random variability and, thus, can help detect variations and discontinuities in the signal such as sudden changes in the retina biological tissue caused by lipid deposits. The latter is an indicator of the regularity of a signal distribution. Therefore, it is suitable to measure the degree of overall homogeneity in retina biological tissue. Together, entropy and uniformity may capture the abrupt and frequent image contrast variations that are observed in the presence of circinate exudates. They are defined by [8]:

$$Entropy = - \sum_{i=0}^{L-1} p(z_i) \log_2 p(z_i) \quad (5)$$

$$Uniformity = \sum_{i=0}^{L-1} p^2(z_i) \quad (6)$$

where z is a random variable for intensity, p is the probability density of the i th pixel in the histogram, and L is the total number of intensity levels.

Feature vector classification

In order to solve a binary classification problem in which the output $y \in \{+1, -1\}$, the SVM [33] implements a hyper-plane $w \cdot \Phi(x) + b = 0$ to separate the data from the classes $+1$ and -1 with a maximal margin. Here, x denotes the input feature vector, w is a weight vector, b is a bias term, and Φ is a function that maps the feature data to a higher dimension space where it is linearly separable. The decision frontier between the two classes is determined with the Lagrange multiplier optimization technique. It is given by:

$$f(x) = \sum_{x_i} y_i \alpha_i \Phi(x_i) \cdot \Phi(x) + b \quad (7)$$

where each α_i is a Lagrange coefficient to be determined from the data. In practice, only the scalar product of Φ by itself is needed in equation 6. Hence, it is not necessary to know Φ if a kernel function provides the result. Then, the optimal decision separating function is:

$$y = \text{sign} \left(\sum_{i=1}^n y_i \alpha_i K(x_i, x) + b \right) \quad (8)$$

where $K(x_i, x)$ is a kernel that replaces the product $\Phi(x_i) \cdot \Phi(x)$. In this study, a polynomial kernel was adopted as its order is only parameter to set. We tried orders from 2 to 4 and found that they provide similar results. Therefore, we chose the second-order kernel for computational efficiency. The second-order kernel is defined as follows:

$$K(x, x_i) = ((x_i \cdot x) + 1)^2 \quad (9)$$

Experimental results and performance evaluation

We evaluated the performance of the proposed circinate exudate detection system with a set of 23 normal images and 22 images with circinate exudates taken from STARE [12], a publicly available dataset. All images are of size 150×130 pixels. The choice of just a subset of STARE was motivated by the fact that this database contains unequal numbers of image types, which may lead to category overfitting and a biased statistical significance of the classifier's results; using equal partitions of normal and abnormal images avoids these problems. The choice of a balanced dataset is also made in [28, 30, 31, 34], in contradiction to other works such as [5, 6], where 27 normal and 90 abnormal images were considered, and [14], where 76 normal and 114 abnormal images were used. Such unbalanced datasets question the relative robustness of the obtained results.

Figures 5 and 6 exhibit example mesh images of the first and second intrinsic mode functions related to normal and circinate exudates images, respectively. The two abnormal IMFs clearly show more high-frequency content than the normal ones, hence, corroborating the hypothesis that the components (intrinsic mode functions) from which the entropy and uniformity statistics are computed are different among normal and abnormal images.

Using tenfold cross-validation, the results were that the proposed circinate exudate detection system achieves

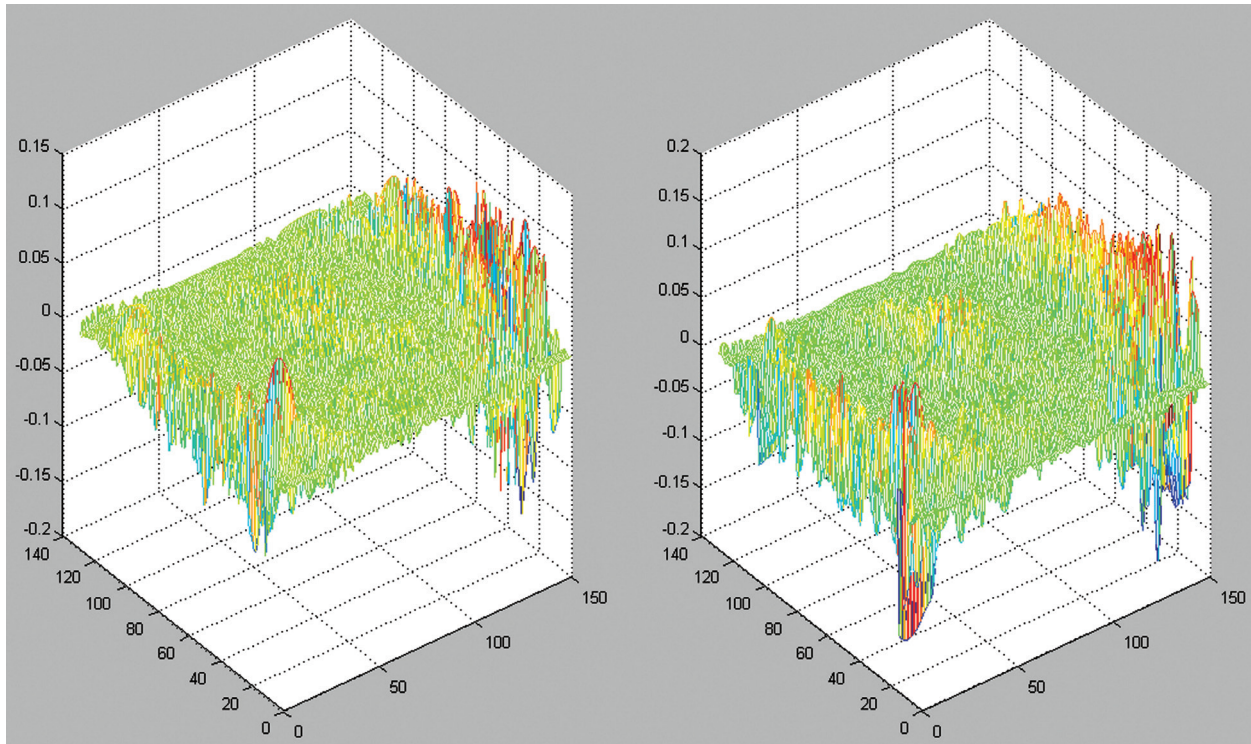


Figure 5 Normal image: first IMF (left) and second IMF (right).

Table 1 Comparison with previous studies.

Study	Approach	Classifier	Performance
[7]	Wavelet decomposition, 80 features, conditional entropy for feature selection	SVM	0.88–0.93 (AUC)
[22]	Color normalization, local contrast enhancement, fuzzy <i>C</i> -means clustering	Neural network	93.4% (accuracy) 93% (sensitivity) 94.1% (specificity)
[36]	Local contrast enhancement, fuzzy <i>C</i> -means	SVM	88% (sensitivity) 84% (specificity)
[21]	Spatial clustering of objects	Expectation maximization algorithm	0.83 (AUC)
[28]	Contextual features, feature selection, 30 most discriminative features	Linear discriminant classifier	0.945 (AUC)
[4]	Multiscale morphological algorithms	Clinical reference standard	95% (sensitivity) 84.6% (specificity)
[34]	High gray level variation, morphological reconstruction, watershed	Human expert	92.8% (sensitivity) 92.4% (specificity)
[31]	Otsu algorithm, morphological reconstruction	Human expert	80% (sensitivity) 99.5% (specificity)
[14]	Adaptive threshold and image partitioning	Human expert	99.5% (accuracy) 91.2% (sensitivity) 99.3% (specificity)
[5, 6]	Global and adaptive histogram thresholding, 18 statistical features	Neural network with radial basis function	92.54% (accuracy) 100% (sensitivity) 81.48% (specificity)
[10]	Grayscale morphology, Chan-Vese level set segmentation, 15 shape features	Naïve Bayes	75% (sensitivity)
[30]	Scale-space extrinsic curvature, local maxima blob response	Human expert	97.07% (sensitivity) 99.90% (specificity)
Our work	EMD+uniformity+entropy	SVM	100% (accuracy) 100% (sensitivity) 100% (specificity) 1 (AUC)

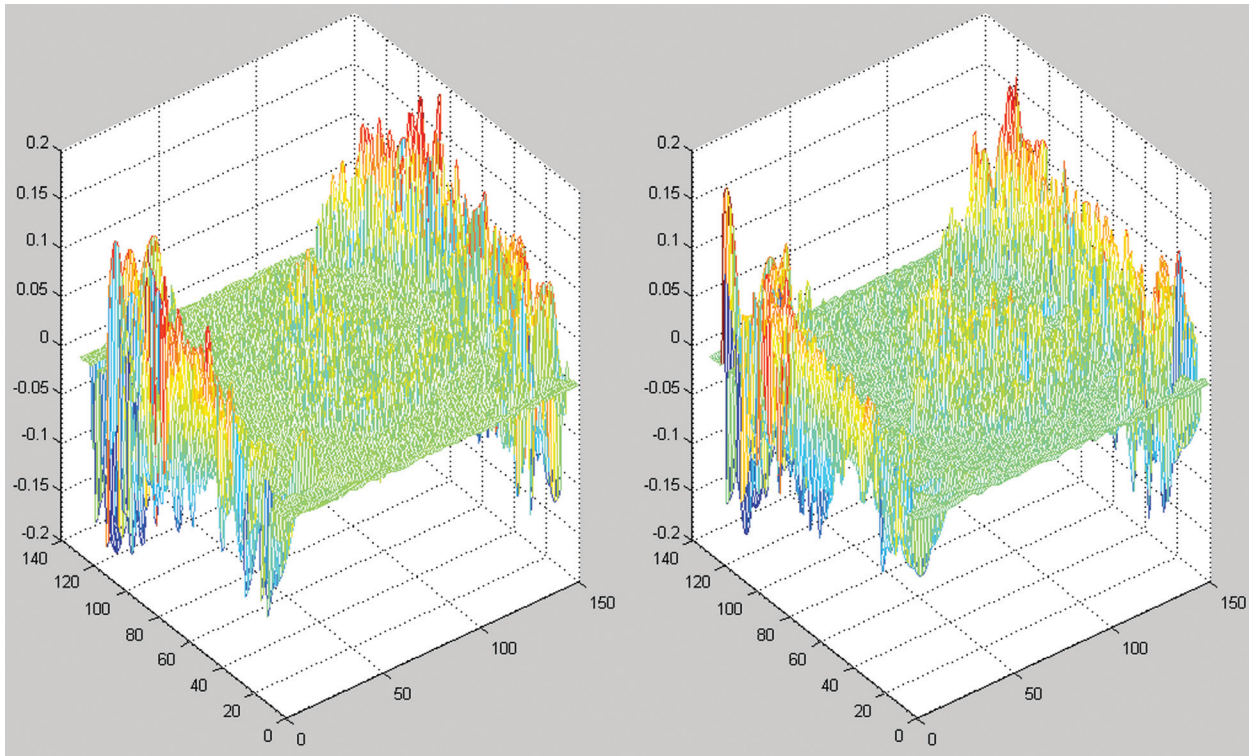


Figure 6 Circinate exudates: first IMF (left) and second IMF (right).

perfect classification accuracy. It is also seen from Table 1 that it outperforms previous comparable studies, which considered only the problem of classification of normal retina images against exudate ones as we did¹ [4, 5, 10, 21, 22, 31, 34, 36]. Furthermore, the system presented here uses only two features to distinguish between healthy retina digital images and unhealthy ones, in contrast to [7] with 80 features, [5] and [6] with 18, [28] with 13, and [10] with 15. It appears then that our retina diagnosis system is simpler to implement.

On the negative side, the obtained performance came at the cost of substantially longer processing time in comparison to other works, due mainly to the envelope interpolation stage in the EMD algorithm. The simulation of EMD with Matlab® R2009a running on a 1.5-GHz Core2 Duo processor, took up to 33 min for normal images and up to 80 min for abnormal images. However, this processing time went down to 193 s on a 3.30-GHz Core™ i5-2500 CPU. Thus, with fast CPU such as the ones used in recent multi-core processing stations, the presented approach for classification of normal against retina with circinate exudates may be suitable for near real-time machine diagnosis.

¹ In [5–7, 10, 30], the main purpose was the segmentation of abnormal images affected with exudates, and the morphology-based studies [4, 14, 31, 34] were evaluated by human experts or by using clinical standards.

Conclusion

This paper described an automated processing system for the detection of circinate exudates in retina digital images. The empirical mode decomposition is applied to an image to obtain the first two intrinsic mode functions, and their entropy and uniformity statistics are computed to form a four-component feature vector that feeds a support vector machine with quadratic kernel. Using ten-fold cross-validation, the system classified correctly all the samples in the STARE database that we used, thereby, outperforming the previous systems described in the literature. The simplicity and relatively fast image processing of the proposed automated circinate exudate detection system make it promising for clinical applications.

The empirical mode decomposition processing time depends on the type of retina image. In particular, an image with circinate exudates takes substantially more processing time than a normal retina image. One may think of reducing the processing time by improving the algorithm of the empirical mode decomposition, particularly the envelope construction step, or by using faster processors than the ones used in this work. Future work should also consider a larger base of retina images to check the consistency of the presented circinate exudates detection system.

Received April 19, 2013; accepted February 11, 2014; online first March 11, 2014

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